

Errors in Differential Equations

Mathematica Differential Equations

1) $d[x1]/dt = 0$

CellML Equations

1) $d[x1]/dt = -v1$

Flux equations relating to differential equations:

1) $v1 \rightarrow (k1*x1[t]*x2[t] - kd1*x3[t])$

$\rightarrow d[x1]/dt = -v1$

BUT

In the paper – says assume no change in $x1$ (EGF) as it is constantly replenished by the blood (ie source term keeps at zero).

Errors in Original CellML code

Original CellML Code:

1) $d[x24]/dt = v17 + v25 + v35 + v40 + v64 + v72 + v130 + v131$

2) $d[x26]/dt = v18 + v21 + v26 + v31 + v65 + v68 + v73 + v78$

3) $d[x69]/dt = v74 + v75 - v66$

4) $d[x82]/dt = -(v96 + v97)$

Actual differential equations (verified against flux equations):

1) $d[x24]/dt = -(v17 + v25 + v35 + v40 + v64 + v72 + v130 + v131)$

2) $d[x26]/dt = -(v18 + v21 + v26 + v31 + v65 + v68 + v73 + v78)$

3) $d[x69]/dt = -(v66 + v74 + v75)$

4) $d[x82]/dt = v96 + v97$

Errors in Kinetic Parameters

Listed in the paper/used in CellML:

1) $k13 = 4.28E+04$

2) $kd18 = 3.80E+04$

3) $k29 = 1.17E-02$

4) $k44 = 1.95E-01$

5) $kd45 = 3.81E+04$

6) $kd47 = 3.82E+04$

- 7) $k_{48} = 2.38E-01$
- 8) $k_{d49} = 5.80E-02$
- 9) $k_{52} = 8.91E-01$
- 10) $k_{d55} = 3.82E+04$
- 11) $k_{58} = 8.33E-02$

Used in Mathematica Model:

Given constants:

- $a = 6 \cdot 10^{23}$
- $V_z = 1 \cdot 10^{-12}$
- $K_{mMEK} = 3 \cdot 10^{-7}$
- $k_{d45} = 3.5$ (see below)
- $k_{d44} = 1.83 \cdot 10^{-2}$
- $k_{48} = 2.38 \cdot 10^{-5}$ (see below)
- $K_{mPase} = 6 \cdot 10^{-8}$
- $k_{d48} = 8 \cdot 10^{-1}$
- $k_{d53} = 16$
- $k_{d52} = 3.3 \cdot 10^{-2}$
- $K_{mERK} = 3 \cdot 10^{-7}$

Equations:

- 1) $k_{13} = 217 \cdot 10^{-2} = 2.17E+00$
- 2) $k_{d18} = 13 \cdot 10^{-1} = 1.30E+00$
- 3) $k_{29} = 7 \cdot 10^5 / a / V_z$
 $= 1.17E-06$
- 4) $k_{44} = (k_{d45} + k_{d44}) / a / V_z / K_{mMEK}$
 $= 1.95E-05$
- 5) $k_{d45} = 35 \cdot 10^{-1} = 3.50E+00$
- 6) $k_{d47} = 29 \cdot 10^{-1} = 2.90E+00$
- 7) $k_{48} = 143 \cdot 10^5 / a / V_z$
 $= 2.38E-05$
- 8) $k_{d49} = k_{48} \cdot a \cdot V_z \cdot K_{mPase} - k_{d48}$
 $= 5.68E-02$
- 9) $k_{52} = (k_{d53} + k_{d52}) / a / V_z / K_{mERK}$
 $= 8.91E-05$
- 10) $k_{d55} = 57 \cdot 10^{-1} = 5.70E+00$
- 11) $k_{58} = 5 \cdot 10^6 / a / V_z$
 $= 8.33E-06$

Errors in Given Equations

Original Equations:

$$\begin{aligned} 1) \quad v_9 &: [(EGF-EGFR^*)_2-GAP] \rightarrow [(EGF-EGFRi^*)_2-GAP] \\ &\rightarrow v_9 = k_6 * c(23) * 1 - kd_6 * c(18) \\ c(23) &= (EGF-EGFR^*)_2-GAP-Grb2 \\ c(18) &= (EGF-EGFRi^*)_2-GAP-Grb2 \end{aligned}$$

Correct Solution:

$$\begin{aligned} 1) \quad c(15) &= (EGF-EGFR^*)_2-GAP \\ c(17) &= (EGF-EGFRi^*)_2-GAP \\ &\rightarrow v_9 = k_6 * c(15) * 1 - kd_6 * c(17) \end{aligned}$$

Required Changes:

$$\begin{aligned} 1) \quad v_9 &= k_6 * c(23) * 1 - kd_6 * c(18) \rightarrow v_9 = k_6 * c(15) * 1 - kd_6 * c(17) \\ &\rightarrow d[x15]/dt = v_8 - (v_9 + v_{16} + v_{22} + v_{32} + v_{34} + v_{37} + v_{39} + v_{102}) \\ &\rightarrow d[x17]/dt = v_{14} + v_{102} - (v_9 + v_{63} + v_{69} + v_{79} + v_{80} + v_{81} + v_{82} + v_{132}) \\ &\rightarrow d[x18]/dt = v_9 + v_{63} - (v_5 + v_{64} + v_{133}) \\ &\rightarrow d[x23]/dt = v_{16} - (v_4 + v_9 + v_{17}) \end{aligned}$$